

# Application-Specific Cryptographic Schemes Based on Symmetric-Key Primitives

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- ① Background and Motivation
- ② Redactable Signature Scheme for Tree-Structured Data
- ③ Forward-Secure Sequential Aggregate Message Authentication

Joint work with Hidenori Kuwakado

# Background and Motivation

Almost all cryptographic protocols/schemes use hash functions.

$$H : \{0, 1\}^* \rightarrow \{0, 1\}^n$$

Security requirements for hash functions:

- (Second-)Preimage resistance (Onewayness)  
 $H$  is easy, and  $H^{-1}$  is difficult.
- Collision resistance  
It is difficult to find distinct  $M, M'$  s.t.  $H(M) = H(M')$ .
- Random oracle  
 $H$  is a random function.
- Pseudorandom function (PRF, for keyed hash functions)  
 $H_K$  is indistinguishable from a random function.

## Problems

- Random oracle is an ideal assumption.
- There exists a large gap between OW and CR [Simon 98]:
  - A CR HF cannot be constructed with a black-box OW permutation.

## Important to identify requirements for hash functions

- Needs multiple requirements?
- Really needs RO?
- Really needs CR?

## Redactable Signature Scheme for Tree-Structured Data Based on Merkle Tree

- Background
- Related Work
- Definition
- Proposed Scheme
- Provable Security

## Database outsourcing with clouds

- Owners of data outsource database service to a provider.

## Security requirements

- Confidentiality of data
  - Unauthorized users should not have access
- Correctness proofs of answers to queries

## Problem

- Efficient processing of encrypted data is difficult
- Unreasonable to prepare signatures of all possible answers in advance
  - Queries are various
  - Access rights are different from users

Useful if signature of data by owner is redactable by provider

## Early work on redactable signature

[Steinfeld, Bull, Zheng 2001] Content extraction signature

[Miyazaki et al. 2003] Digital document sanitization

- The owner
  - ① divides documents into parts
  - ② signs commitments of all parts of a document
- The provider reveals some parts to users
  - according to their access rights
  - without using owner's signing key

### Redactable signature for tree-structured data

For tree-structured data and its signature,  
signatures of subtrees are computable without the signing key

[Kundu, Bertino 2008] First scheme, turned out insecure

[Bruzska et al. 2010]

- Formal definitions of security requirements
- Scheme using ordinary signature

[Samelin et al. 2012], [Pöhls et al. 2012]

- Allow more flexible redaction  
Eg.: Removal of internal node(s)

These schemes are inefficient:

- Signing requires  $\Omega(N)$  calls to ordinary signing.
- $N$ : Number of nodes of the tree



Redactable signature scheme for tree-structured data

- Based on Merkle tree
- Signing involves **only one** call to ordinary signing procedure
- Provably secure

☹ The proposed scheme can be applied to tree-structured data with  
Out-degree  $\leq$  constant (chosen by application)

# Redactable Signature Scheme for Tree-Structured Data

$$\text{tSig} = (\text{tK}, \text{tS}, \text{tV}, \text{tC})$$

**Key generation**  $(sk, pk) \leftarrow \text{tK}(1^\ell)$

$\ell$  is a security parameter

**Signing**  $(T, \sigma) \leftarrow \text{tS}(sk, T)$

$\sigma$  is a signature for tree-structured data  $T$

**Verification**  $d \leftarrow \text{tV}(pk, T, \sigma)$

$$d = \begin{cases} 1 & \text{if } \sigma \text{ is a valid signature for } T \text{ w.r.t. } pk \\ 0 & \text{otherwise} \end{cases}$$

**Cutting**  $(T', \sigma') \leftarrow \text{tC}(pk, T, \sigma, L)$

$L$  is a leaf of  $T$

$\sigma'$  is a signature for  $T' = T \setminus L$

The secret signing key  $sk$  is not used

Multiple cutting produces signature of any sub-tree sharing the root with  $T$

[Bruzska et al. 2010]

## Unforgeability

Similar to **EUF-CMA** of ordinary signature

Existential UnForgeability against adaptive Chosen Message Attacks

**Difference: Redaction is not forgery**

## Transparency

Formalized by impossibility to tell whether a signature is created

- only by signing, or
- by first signing, and then cutting

**Impossible to tell whether cutting is carried out or not after signing**

- **No information is leaked on the deleted parts (if any)**



# Transparency

$\mathcal{A}$	Adversary	tK	Key generation algorithm
		tS	Signing algorithm
		tC	Cutting algorithm

## Experiment

```
 $(sk, pk) \leftarrow \text{tK}(1^\ell)$   
 $b \leftarrow \{0, 1\}$   
 $d \leftarrow \mathcal{A}^{\text{tS}(sk, \cdot), \text{SorC}(\cdot, \cdot, sk, b)}(pk)$   
if  $d = b$  then  
    Success  
else  
    Failure
```

```
function  $\text{SorC}(T, L, sk, b)$   
    if  $b = 0$  then  
         $(T, \sigma) \leftarrow \text{tS}(sk, T)$   
         $(T', \sigma') \leftarrow \text{tC}(pk, T, \sigma, L)$   
    else  
         $T' \leftarrow T \setminus L$   
         $(T', \sigma') \leftarrow \text{tS}(sk, T')$   
    return  $(T', \sigma')$ 
```

Transparent  $\Leftrightarrow \left| \Pr[\text{Success}] - 1/2 \right|$  is negligible

## Proposed Scheme (Signing Algorithm)

$H$  hash function

$K$  master secret key (for transparency)

$r$  nonce

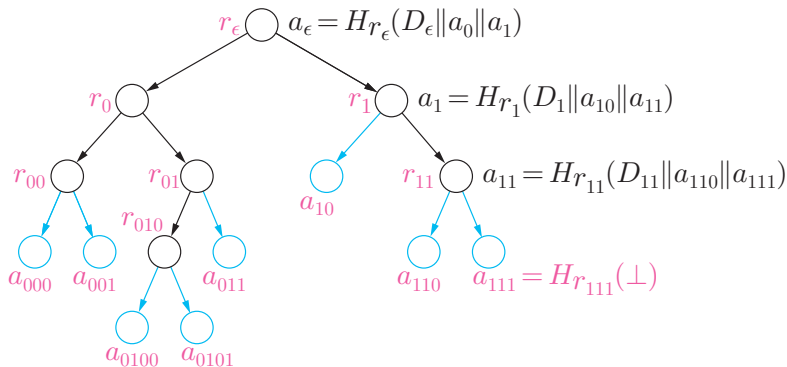
Let out-degree  $\leq d$

- 1 (Construction of Merkle tree) For a given tree  $T$ ,
  - 1 Construct tree  $T'$  by adding dummy child nodes and edges for nodes (including leaves) with out-degree  $< d$
  - 2 For each node  $v_i$  of  $T'$ , compute secret key  $r_i = H_K(r||i)$
  - 3 Construct Merkle tree using  $H_{r_i}$  for node  $v_i$
- 2 Sign the root digest using an ordinary signature scheme

# Signing Algorithm (with Example of Merkle Tree, out-deg. $\leq 2$ )

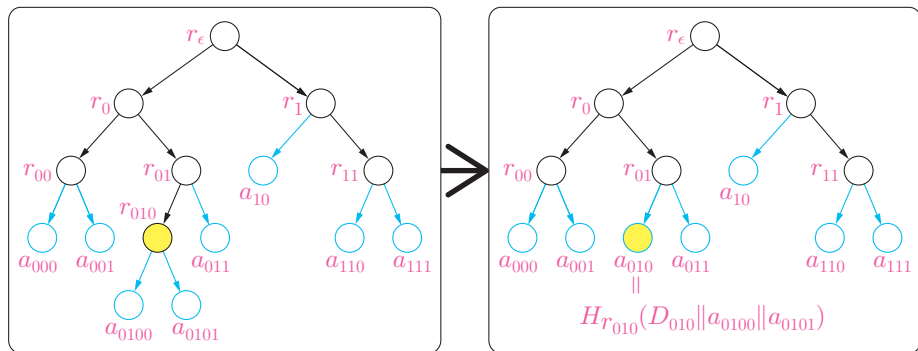
The signature of  $T$  (drawn with black) is a tuple of

- Signature of the root digest  $a_\epsilon$
- Digests  $a_i = H_{r_i}(\perp)$  of all dummy nodes (drawn with blue)
- Secret keys  $r_i = H_K(r\|i)$  corresponding to nodes  $v_i$  of  $T$



# Cutting Algorithm (Example)

The leaf  $v_{010}$  (yellow) is cut:  $v_{010}$  becomes a dummy node.



New signature is obtained by

- 1 removing secret key  $r_{010}$  and digests  $a_{0100}$ ,  $a_{0101}$  from the original
- 2 adding  $a_{010} = H_{r_{010}}(D_{010} || a_{0100} || a_{0101})$



# Provable Security of Proposed Scheme

tSig proposed scheme

Sig ordinary signature scheme for root digest

$H$  hash function

## Theorem (Unforgeability)

$(\text{Sig is unforgeable}) \wedge (H \text{ is collision resistant}) \Rightarrow \text{tSig is unforgeable}$

- Unforgeability of Sig avoids forgery of signature for new root digests.
- CR of  $H$  avoids generation of Merkle trees with the same root digest.

## Theorem (Transparency)

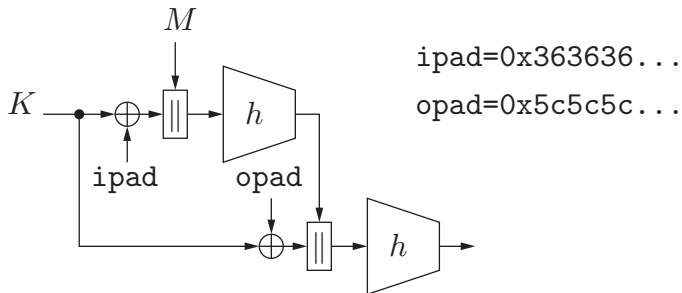
$\text{Keyed mode of } H \text{ is a pseudorandom function} \Rightarrow \text{tSig is transparent}$

- Digests of nodes look random due to the PRF property of  $H_K$ .

HMAC can instantiate the HF  $H$  in the proposed scheme:

- Used as a pseudorandom function
- Hash function  $h$  is collision-resistant (CR)  $\Rightarrow$  HMAC is CR

MAC (Message Authentication Code) function using a hash function



Redactable signature scheme for tree-structured data

- Based on Merkle tree using keyed hash function such as HMAC
  - efficient, but
  - out-degree  $\leq \text{const}$
- Provable security (unforgeability & transparency)
- Extension to DAG (Directed Acyclic Graph) is straightforward.

Future work

Efficient & provably secure scheme for

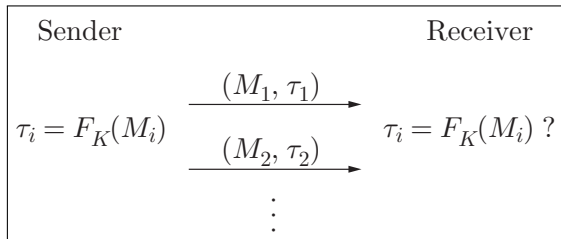
- more general tree
- graph

# Forward-Secure Sequential Aggregate Message Authentication Revisited

- Background
- Related Work
- Definition
- Proposed Scheme
- Provable Security

## Message authentication

- MAC function  $F$  should be unforgeable



Applications such as secure logging and sensor networks require

- forward secrecy (for the case of secret-key leakage)
- detection of reordering and deletion
- reduction of resource consumption (memory, transmission power, ...)

FS SAMA [Ma, Tsudik 2007]

## Forward Secure

- Impossible to forge tags for keys before leakage
- Achieved by secret-key update

## Sequential

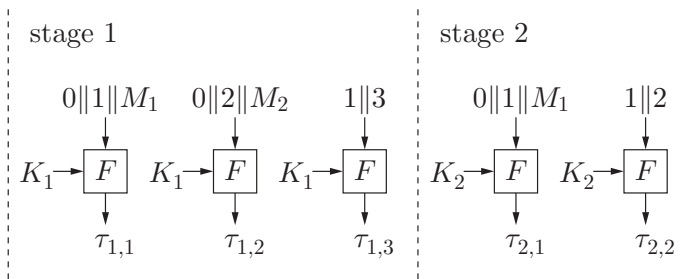
- Reordering and deletion are detectable

## Aggregate

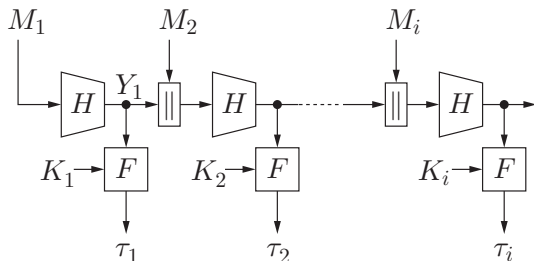
- Tags for messages are aggregatable
- Single tag for a sequence of messages

## Related work

- Forward secure message authentication for audit logs  
[Bellare, Yee 1997], [Schneier, Kelsey 1999]
- History-free message authentication  
[Eikemeier et al. 2010]

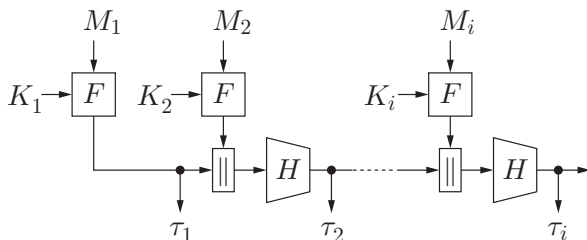


- Numbering scheme
- $F$  is a MAC function.
- $K_i$  is used during stage  $i$ .
- Reordering and deletion are detected by
  - message-numbering,
  - end-marker.
- Aggregation is not considered.

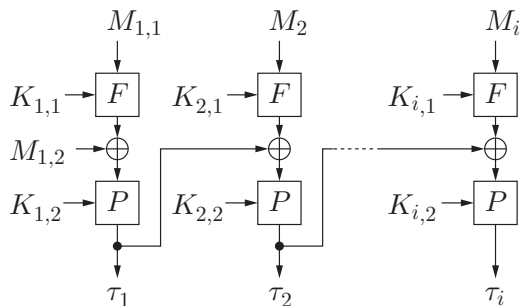


- Linking scheme
- $F$  is a MAC function.
- $H$  is a collision-resistant hash function.  
It is difficult to find distinct  $X, X'$  such that  $H(X) = H(X')$ .
- The secret key is updated after each tagging operation.
- Aggregation is possible.  
 $\tau_i$  is a tag for  $(M_1, \dots, M_i)$ .





- Linking scheme
- $F$  is a MAC function.
- $H$  is a collision-resistant hash function.
- The secret key is updated after each tagging operation.
- Aggregation is possible.



- Linking scheme
- $F$  is a MAC function.
- $P$  is a PRP (pseudorandom permutation)
- The keys for  $F$  are independent of the keys for  $P$ .
- More flexible aggregation is possible.
- Forward secrecy is not considered.

# Our Contribution

- Formalization of scheme and security
- New scheme without CR HF and PRP
- Reduction of the security of the scheme to
  - indistinguishability of the key generator, and
  - unforgeability or indistinguishability of the MAC function

Comparison with previous schemes

Scheme	Aggregation	Col. Resis.	PRP	ProvSec
Bellare-Yee	☹	✓	✓	✓
Schneier-Kelsey	✓	☹	✓	?
Ma-Tsudik	✓	☹	✓	?
Eikemeier et al.	✓✓	✓	☹	✓
Ours	✓	✓	✓	✓

## FS SAMA: Definition (1/2)

SAM = (kgen, update, tag, verif, aggre,  $n$ ),  $n$  is the number of stages

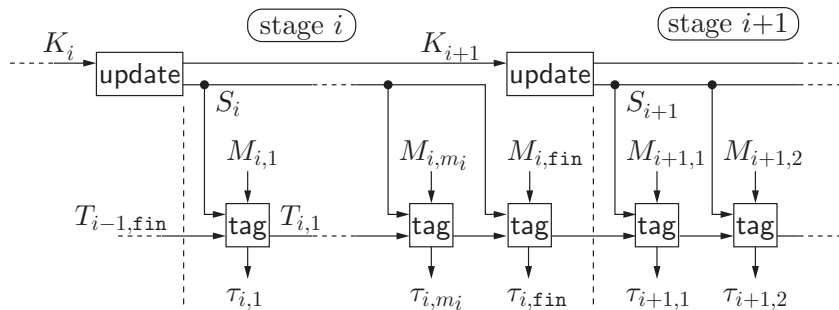
**Key Generation**  $K_1 \leftarrow \text{kgen}(1^\ell)$ ,  $\ell$  is a security parameter.

**Key Update**  $(S_i, K_{i+1}) \leftarrow \text{update}(K_i)$  ( $1 \leq i \leq n$ )

- $S_i$  is a key for tagging during the  $i$ -th stage.

**Tagging**  $(\langle \tau_{i,j}, i \rangle, T_{i,j}) \leftarrow \text{tag}(S_i, T_{i,j-1}, M_{i,j})$  ( $1 \leq i \leq n$ )

- $\tau_{i,j}$  is a tag for message  $M_{i,j}$ .
- $T_{i,j}$  is a state.



## FS SAMA: Definition (2/2)

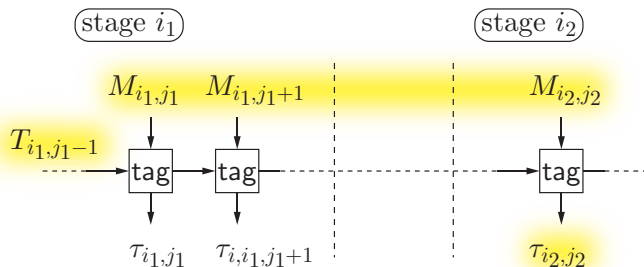
**Verification**  $\alpha \leftarrow \text{verif}(S_{[i_1, i_2]}, T_{i_1, j_1-1}, \mathbf{M}_{[(i_1, j_1), (i_2, j_2)]}, \langle \tau_{i_2, j_2}, i_2 \rangle)$

- $\mathbf{M}_{[(i_1, j_1), (i_2, j_2)]} = (M_{i_1, j_1}, \dots, M_{i_2, j_2})$  is a sequence of messages.

**Aggregation**  $(T_{i_1, j_1-1}, \mathbf{M}_{[(i_1, j_1), (i_2, j_2)]}, \langle \tau_{i_2, j_2}, i_2 \rangle)$

$\leftarrow \text{aggre}(T_{i_1, j_1-1}, \mathbf{M}_{[(i_1, j_1), (i_2, j_2)]}, \boldsymbol{\tau}_{[(i_1, j_1), (i_2, j_2)]})$

- Considers aggregation across stages
- Straightforward from the verification algorithm
- $\boldsymbol{\tau}_{[(i_1, j_1), (i_2, j_2)]} = (\langle \tau_{i_1, j_1}, i_1 \rangle, \dots, \langle \tau_{i_2, j_2}, i_2 \rangle)$  is a sequence of tags for  $\mathbf{M}_{[(i_1, j_1), (i_2, j_2)]}$ .

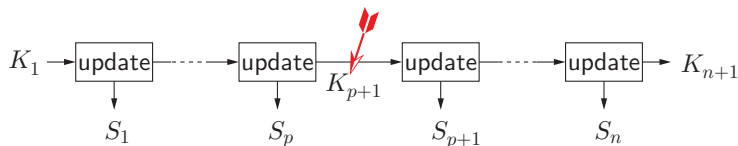


# FS SAMA: Definition of Security

$\text{Exp}_{\text{SAM}, \mathcal{A}}^{\text{fs-samac}}$

Adversary  $\mathcal{A}$

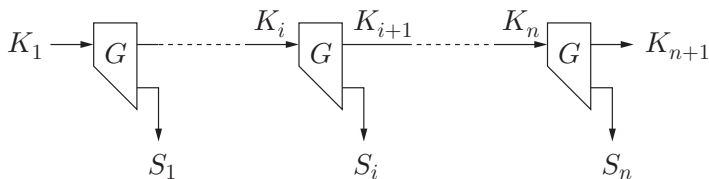
- ① (Up to the  $p$ -th stage)  $\triangleright \mathcal{A}$  is allowed to choose  $p$  arbitrarily.
  - ①  $(S_i, K_{i+1}) \leftarrow \text{update}(K_i)$
  - ② Makes queries to  $\text{tag}(S_i, \cdot, \cdot)$  and gets pairs of a message and a tag.
- ② Obtains  $K_{p+1}$ .
- ③ Produces a pair of message sequence and tag for key  $S_i$  with  $i \leq p$ .



$$\text{Adv}_{\text{SAM}}^{\text{fs-samac}}(\mathcal{A}) = \Pr[\mathcal{A} \text{ succeeds in forgery}]$$

## Proposed Scheme: Key Update

Forward Secure Pseudorandom Generator (FSPRG) [Bellare, Yee 2003]



**Th.** Suppose that  $G$  is PRG.

$K_1$  is chosen uniformly at random

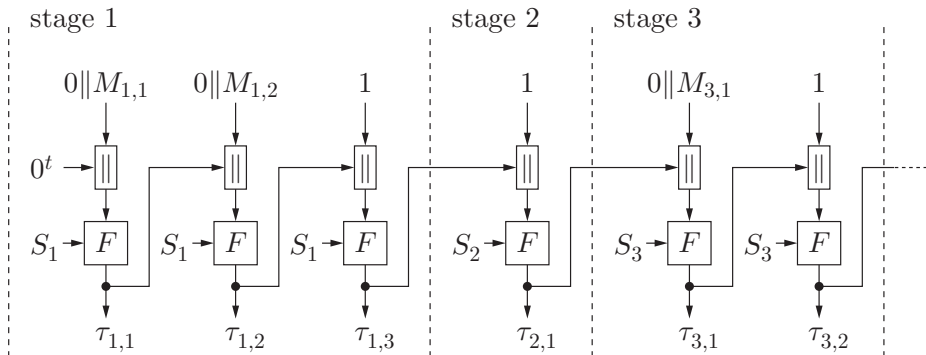
$\Downarrow$

$S_1 \parallel \cdots \parallel S_i$  looks uniformly random even if  $K_{i+1}$  is disclosed

**Def.**  $G$  is PRG.

$K_i$  is chosen uniformly at random  $\Rightarrow K_{i+1} \parallel S_i$  looks uniformly random

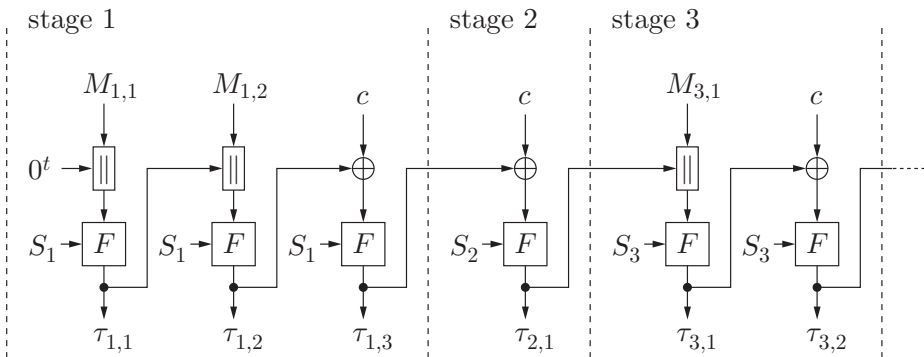
# Proposed Scheme: Tagging



- $F$  is a MAC function
- $S_i$  is used for stage  $i$
- “ $0^t$ ” is the initial state
- “ $1$ ” is the end marker, which prevents truncation attacks
- Tag  $\tau_{i,j}$  is also used as state.



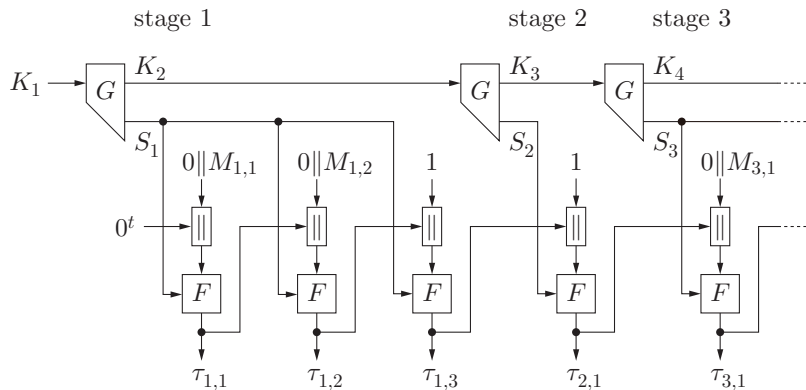
# Tagging: Some Tweak



- $c$  is a non-zero constant.

We have presented two kinds of security reductions:

- to unforgeability of  $F$  and PRG property of  $G$
- to PRF property of  $F$  and PRG property of  $G$



## Security: Reduction to Unforgeability

**Th.** For any adversary  $\mathcal{A}$  against  $\text{SAM}[F, G, n]$  with

$$\mu = (\text{no. of } \mathcal{A}\text{'s queries}) + (\text{no. of messages in } \mathcal{A}\text{'s output})$$

there exists  $\mathcal{B}$  against  $F$  and  $\mathcal{D}$  against  $G$  such that

$$\text{Adv}_{\text{SAM}[F,G,n]}^{\text{fs-samac}}(\mathcal{A}) \leq \frac{n\mu(\mu + 3)}{2} \text{Adv}_F^{\text{mac}}(\mathcal{B}) + 2n \cdot \text{Adv}_G^{\text{prg}}(\mathcal{D})$$

where

- Number of  $\mathcal{B}$ 's queries  $\leq \mu$
- Running time of  $\mathcal{B} \approx$  Running time of  $\text{Exp}_{\text{SAM}[F,G,n],\mathcal{A}}^{\text{fs-samac}}$
- Running time of  $\mathcal{D} \approx$  Running time of  $\text{Exp}_{\text{SAM}[F,G,n],\mathcal{A}}^{\text{fs-samac}}$

## Security: Reduction to Indistinguishability

**Th.** For any adversary  $\mathcal{A}$  against  $\text{SAM}[F, G, n]$  with

$$\mu = (\text{no. of } \mathcal{A}\text{'s queries}) + (\text{no. of messages in } \mathcal{A}\text{'s output})$$

there exists  $\mathcal{C}$  against  $F$  and  $\mathcal{D}$  against  $G$  such that

$$\text{Adv}_{\text{SAM}[F,G,n]}^{\text{fs-samac}}(\mathcal{A}) \leq n \cdot \text{Adv}_F^{\text{prf}}(\mathcal{C}) + 2n \cdot \text{Adv}_G^{\text{prg}}(\mathcal{D}) + \frac{\mu^2 + \mu + 2}{2^{t+1}}$$

where

- Number of  $\mathcal{C}$ 's queries  $\leq \mu$
- Running time of  $\mathcal{C} \approx$  Running time of  $\text{Exp}_{\text{SAM}[F,G,n],\mathcal{A}}^{\text{fs-samac}}$
- Running time of  $\mathcal{D} \approx$  Running time of  $\text{Exp}_{\text{SAM}[F,G,n],\mathcal{A}}^{\text{fs-samac}}$

# Comparison of the Reductions

$$\text{Adv}_{\text{SAM}[F,G,n]}^{\text{fs-samac}}(\mathcal{A}) \leq \frac{n\mu(\mu+3)}{2} \text{Adv}_F^{\text{mac}}(\mathcal{B}) + 2n \cdot \text{Adv}_G^{\text{prg}}(\mathcal{D})$$

$$\text{Adv}_{\text{SAM}[F,G,n]}^{\text{fs-samac}}(\mathcal{A}) \leq n \cdot \text{Adv}_F^{\text{prf}}(\mathcal{C}) + 2n \cdot \text{Adv}_G^{\text{prg}}(\mathcal{D}) + \frac{\mu^2 + \mu + 2}{2^{t+1}}$$

$\frac{n\mu(\mu+3)}{2} \gg n$ , but forgery seems much more difficult than distinction:

$$\text{Adv}_F^{\text{mac}}(\mathcal{B}) \ll \text{Adv}_F^{\text{prf}}(\mathcal{C}) \Leftarrow \mathcal{B}' \text{ s power} \approx \mathcal{C}' \text{ s power}$$

## Forward-Secure Sequential Aggregate Message Authentication

- Gave formalization
- Proposed a new scheme
  - with a MAC function and a PRG
  - without collision-resistant hash functions and PRPs
- Reduced the security of the scheme to
  - indistinguishability of the PRG
  - unforgeability or indistinguishability of the MAC function